

CHAPTER 6--PROBABILITY

TREE DIAGRAMS AND CONSECUTIVE EVENTS

Legend:

N = Notes—copy this in your notebook

A = Activity—I will be explaining and we will do an activity

G = Game—Time to play a Math Game!

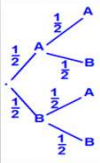
C = Classwork, grab a binder, start now and finish it for homework, look up the worksheet/assignment on.MHS

N Tree Diagrams and Consecutive Events

New terms

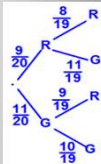
Consecutive events: are two or more events that happen one after another.

With replacement: the first event will have no effect on the next event. ex. Flipping a coin twice



N

Without replacement: the first event will affect the probability of the next event. ex. Picking two marbles from a bag of red and green marbles (once we take a gum ball out of the machine, we do not put it back in for the next draw).



A Gizmos Independent and Dependent Events

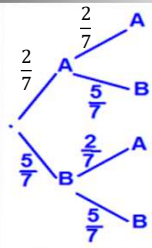
<https://www.explorellearning.com/index.cfm?method=cResource.dspView&ResourceID=249>

Explore:

1. Changing between with replacement and without replacement
2. Changing between 2, 3, and 4 draws

N Example 1: Given the tree diagram below, find P_{AA}.

(Must recognize: "with replacement" because denominator does not change.)



$P(AA) = \frac{2}{7} \cdot \frac{2}{7} = \frac{4}{49}$
 $P(AB) = \frac{2}{7} \cdot \frac{5}{7} = \frac{10}{49}$
 $P(BA) = \frac{5}{7} \cdot \frac{2}{7} = \frac{10}{49}$
 $P(BB) = \frac{5}{7} \cdot \frac{5}{7} = \frac{25}{49}$

Vertical (up and down the tree diagram) = adds up to 1

Horizontal (across the tree diagram) = multiply

N **Example 2:** If a coin is flipped twice, what is the probability of getting a different result on each toss?
 (Must recognize: with replacement because H or T are both options each time you flip a coin)

$P_{HH} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{HT} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{TH} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{TT} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $\frac{1}{4} + \frac{1}{4} = \frac{2}{4} = \frac{1}{2}$

N **Example 3:** In a bag of fruit, there are apples and bananas. If there are 4 apples and 6 bananas, what is the probability of picking an apple on two consecutive draws if there is no replacement?
 (Must recognize: "without replacement" because question says so.)

$P(AA) = \frac{4}{10} \cdot \frac{3}{9} = \frac{3}{9}$
 $P(AB) = \frac{4}{10} \cdot \frac{6}{9} = \frac{24}{90}$
 $P(BA) = \frac{6}{10} \cdot \frac{4}{9} = \frac{24}{90}$
 $P(BB) = \frac{6}{10} \cdot \frac{5}{9} = \frac{30}{90}$

$P(A) = \frac{\# \text{ of apples}}{\# \text{ of fruit}} = \frac{4}{10}$
 $P(B) = \frac{\# \text{ of bananas}}{\# \text{ of fruit}} = \frac{6}{10}$ } do not reduce

N **Example 4:** A bag of marbles has 3 red marbles and 4 blue marbles. What is the probability of selecting different colored marbles on two consecutive draws if we do not replace the marble we drew on the first draw?
 (Must recognize: without replacement because the questions says so).

$P_{RR} = \left(\frac{3}{7}\right)\left(\frac{2}{6}\right) = \frac{6}{42}$
 $P_{RB} = \left(\frac{3}{7}\right)\left(\frac{4}{6}\right) = \frac{12}{42}$
 $P_{BR} = \left(\frac{4}{7}\right)\left(\frac{3}{6}\right) = \frac{12}{42}$
 $P_{BB} = \left(\frac{4}{7}\right)\left(\frac{3}{6}\right) = \frac{12}{42}$
 $\frac{12}{42} + \frac{12}{42} = \frac{24}{42} = \frac{4}{7}$

$P(R) = \frac{\# \text{ of reds}}{\text{total \# of marbles}} = \frac{3}{7}$
 $P(B) = \frac{\# \text{ of blues}}{\text{total \# of marbles}} = \frac{4}{7}$

N **Example 5:** A coin is flipped twice. What is the probability of not getting a head on either toss?
 (Must recognize: with replacement because it's a coin).

$P_{HH} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{HT} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{TH} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$
 $P_{TT} = \left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$

$P(H) = \frac{1}{2}$ and $P(T) = \frac{1}{2}$

C **Classwork/Homework**

Green Binders
 Chapter 6—Probability
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